

An example of CAESAR II Maximum Stress Intensity Calculation

(Input in yellow)

Geometry (input)

$$OD := 6.625\text{-in}$$

$$\text{wall} := 0.28\text{-in}$$

$$ca := 0\text{-in}$$

$$SIFi := 2.218$$

$$SIFo := 2.218$$

$$FAC := 1$$

(use of corrosion is stress type specific)

(SIF multiplier is stress type specific)

Geometry Calcs.

$$wt := \text{wall} - ca$$

$$ID := OD - 2 \cdot wt$$

$$A_{\text{net}} := \frac{\pi}{4} \cdot (OD^2 - ID^2)$$

$$I := \frac{\pi}{64} \cdot (OD^4 - ID^4)$$

$$Ro := \frac{OD}{2}$$

$$Z := \frac{I}{Ro}$$

Loads (input)

$$P := 100\text{-psi}$$

$$Fax := -279\text{-lbf}$$

$$Mi := 2057\text{-ft}\cdot\text{lbf}$$

$$Mo := -147.9\text{-ft}\cdot\text{lbf}$$

$$T_{\text{net}} := 202.1\text{-ft}\cdot\text{lbf}$$

Stresses:

Set stress intensification factors

$$ii := \text{if}(FAC \cdot SIFi > 1, FAC \cdot SIFi, 1) \quad ii = 2.218$$

$$io := \text{if}(FAC \cdot SIFo > 1, FAC \cdot SIFo, 1) \quad io = 2.218$$

$$Slp := \frac{P \cdot ID^2}{OD^2 - ID^2} \quad Slp = 518\text{ psi}$$

$$\sigma_{\text{hoop}} := \frac{P \cdot ID}{2 \cdot wt} \quad \sigma_{\text{hoop}} = 1083\text{ psi} \quad (\text{hoop stress calc. varies according to configuration setting: ID, OD, mean, Lamé})$$

$$\sigma_{\text{axial}} := Slp + \frac{Fax}{A} \quad \frac{Fax}{A} = -50\text{ psi} \quad \sigma_{\text{axial}} = 468\text{ psi}$$

$$Sb := \frac{\sqrt{(ii \cdot Mi)^2 + (io \cdot Mo)^2}}{Z} \quad Sb = 6461\text{ psi}$$

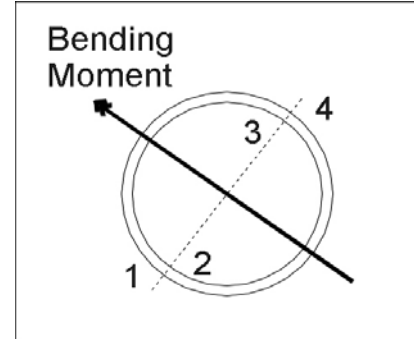
$$\tau := \frac{T}{2 \cdot Z} \quad \tau = 143\text{ psi}$$

$$\sigma := Slp + \frac{Fax}{A} + Sb \quad \sigma = 6929\text{ psi}$$

Assemble the stress components required to calculate the three dimensional stress intensity at four locations through the pipe wall.

Calculate the stresses along the pipe diameter which is perpendicular to the resultant bending moment.

- 1: outside surface, moment causes tension
- 2: inside surface, moment causes tension
- 3: inside surface, moment causes compression
- 4: outside surface, moment causes compression



Intermediate calc's:

$$R_i := \frac{ID}{2} \quad A_{in} := \frac{\pi}{4} \cdot ID^2 \quad A_{xs} := A$$

$$axial := P \cdot A_{in} + Fax \quad bend := \sqrt{(ii \cdot M_i)^2 + (io \cdot M_o)^2}$$

longitudinal stress

hoop stress

radial stress (force this term negative)

shear stress

$$\sigma_l := \begin{pmatrix} \frac{axial}{A_{xs}} + \frac{bend \cdot Ro}{I} \\ \frac{axial}{A_{xs}} + \frac{bend \cdot Ri}{I} \\ \frac{axial}{A_{xs}} - \frac{bend \cdot Ri}{I} \\ \frac{axial}{A_{xs}} - \frac{bend \cdot Ro}{I} \end{pmatrix}$$

$$\sigma_h := \begin{pmatrix} P \cdot \frac{R_i^2}{(R_o^2 - R_i^2)} \cdot \left(\frac{R_o^2}{R_o^2} + 1 \right) \\ P \cdot \frac{R_i^2}{(R_o^2 - R_i^2)} \cdot \left(\frac{R_o^2}{R_i^2} + 1 \right) \\ P \cdot \frac{R_i^2}{(R_o^2 - R_i^2)} \cdot \left(\frac{R_o^2}{R_i^2} + 1 \right) \\ P \cdot \frac{R_i^2}{(R_o^2 - R_i^2)} \cdot \left(\frac{R_o^2}{R_o^2} + 1 \right) \end{pmatrix}$$

$$\sigma_r := \begin{pmatrix} 0 \\ -P \\ -P \\ 0 \end{pmatrix}$$

$$\tau_{\theta z} := \begin{pmatrix} \frac{T \cdot Ro}{2 \cdot I} \\ \frac{T \cdot Ri}{2 \cdot I} \\ \frac{T \cdot Ri}{2 \cdot I} \\ \frac{T \cdot Ro}{2 \cdot I} \end{pmatrix}$$

Sa and Sb are the principal 2D stresses in the plane normal to the radial direction, Sc is radial.

$$S_{a(p)} := \frac{\sigma_{lp} + \sigma_{hp}}{2} + \frac{\sqrt{(\sigma_{lp} - \sigma_{hp})^2 + (2 \cdot \tau_p)^2}}{2} \quad S_{b(p)} := \frac{\sigma_{lp} + \sigma_{hp}}{2} - \frac{\sqrt{(\sigma_{lp} - \sigma_{hp})^2 + (2 \cdot \tau_p)^2}}{2} \quad S_{c(p)} := \sigma_{rp}$$

Principal stresses at positions 1 to 4

$$S_q := \begin{pmatrix} S_a(1) & S_a(2) & S_a(3) & S_a(4) \\ S_b(1) & S_b(2) & S_b(3) & S_b(4) \\ S_c(1) & S_c(2) & S_c(3) & S_c(4) \end{pmatrix}$$

$$S_q = \begin{pmatrix} 6.932 \times 10^3 & 6.386 \times 10^3 & 1.138 \times 10^3 & 1.038 \times 10^3 \\ 1.032 \times 10^3 & 1.132 \times 10^3 & -5.45 \times 10^3 & -5.996 \times 10^3 \\ 0 & -100 & -100 & 0 \end{pmatrix} \text{ psi}$$

sort stresses at each position (first in ascending order, then in reverse order)

$$Q(p) := \text{sort}(S_q^{(p)}) \quad S_w(p) := \text{reverse}(Q(p))$$

$$S(1) = \begin{pmatrix} 6932 \\ 1032 \\ 0 \end{pmatrix} \text{psi} \quad S(2) = \begin{pmatrix} 6386 \\ 1132 \\ -100 \end{pmatrix} \text{psi} \quad S(3) = \begin{pmatrix} 1138 \\ -100 \\ -5450 \end{pmatrix} \text{psi} \quad S(4) = \begin{pmatrix} 1038 \\ 0 \\ -5996 \end{pmatrix} \text{psi}$$

maximum principal stress (S1) at position "p"

$$S1(p) := S(p)_1 \quad S1(1) = 6932 \text{psi} \quad S1(2) = 6386 \text{psi} \quad S1(3) = 1138 \text{psi} \quad S1(4) = 1038 \text{psi}$$

$$S2(p) := S(p)_2 \quad S2(1) = 1032 \text{psi} \quad S2(2) = 1132 \text{psi} \quad S2(3) = -100 \text{psi} \quad S2(4) = 0 \text{psi}$$

minimum principal stress (S3) at position "p"

$$S3(p) := S(p)_3 \quad S3(1) = 0 \text{psi} \quad S3(2) = -100 \text{psi} \quad S3(3) = -5450 \text{psi} \quad S3(4) = -5996 \text{psi}$$

SI:: Maximum Shear Stress Intensity at position "p"

$$SI(p) := S1(p) - S3(p) \quad _3DMax := \begin{pmatrix} SI(1) \\ SI(2) \\ SI(3) \\ SI(4) \end{pmatrix} \quad \text{MaxStressIntensity} := \max(_3DMax)$$

$$\text{MaxStressIntensity} = 7034 \text{psi}$$

In non-fatigue applications, maximum stress intensity is limited by material yield stress. (Actually, maximum shear stress which is half of the stress intensity is limited by one half of yield.)